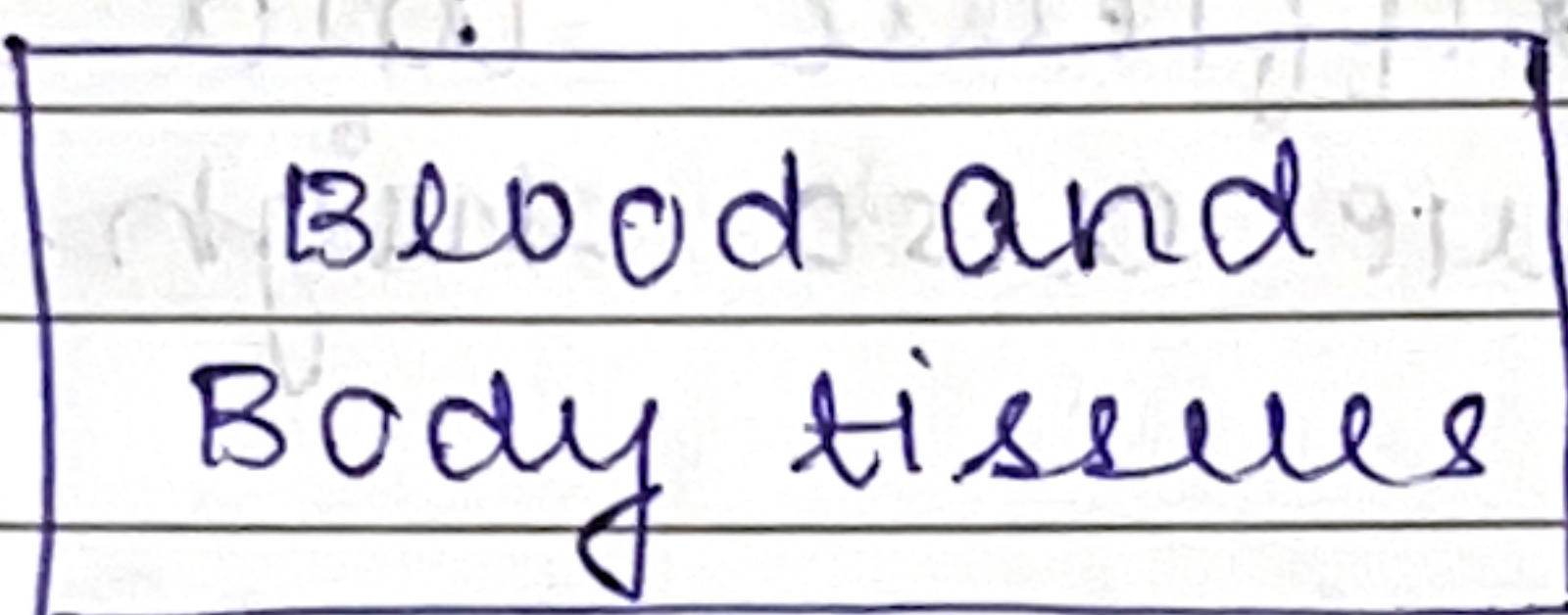


## ONE COMPARTMENT OPEN MODEL (IV BOLUS) :

- When drug is given by rapid iv injection, it distributes rapidly and takes about one to three minutes for complete circulation.
- This neglects its rate of absorption.



→  $k_e$

- General expression :

$$\frac{dx}{dt} = \text{Rate in} - \text{Rate out}$$

Here, Rate-in or absorption is absent.

The equation becomes:

$$\frac{dx}{dt} = - \text{Rate out}$$

∴ If rate-out follows first order kinetics, then:

$$\frac{dx}{dt} = -k_e x$$

Where,

$k_e$  = 1st order elimination.

$x$  = Amt. of drug in body

(1)



Pharmacokinetic parameters :  
 (1) Elimination rate constant -

Integration of eq (1)

$$\ln x = \ln x_0 - k_{el} t \quad \text{--- (2)}$$

Express eq (2) in exponential form:

$$x = x_0 e^{-k_{el} t} \quad \text{--- (3)}$$

Transforming eq (3) into common logarithms (log base 10), we get:

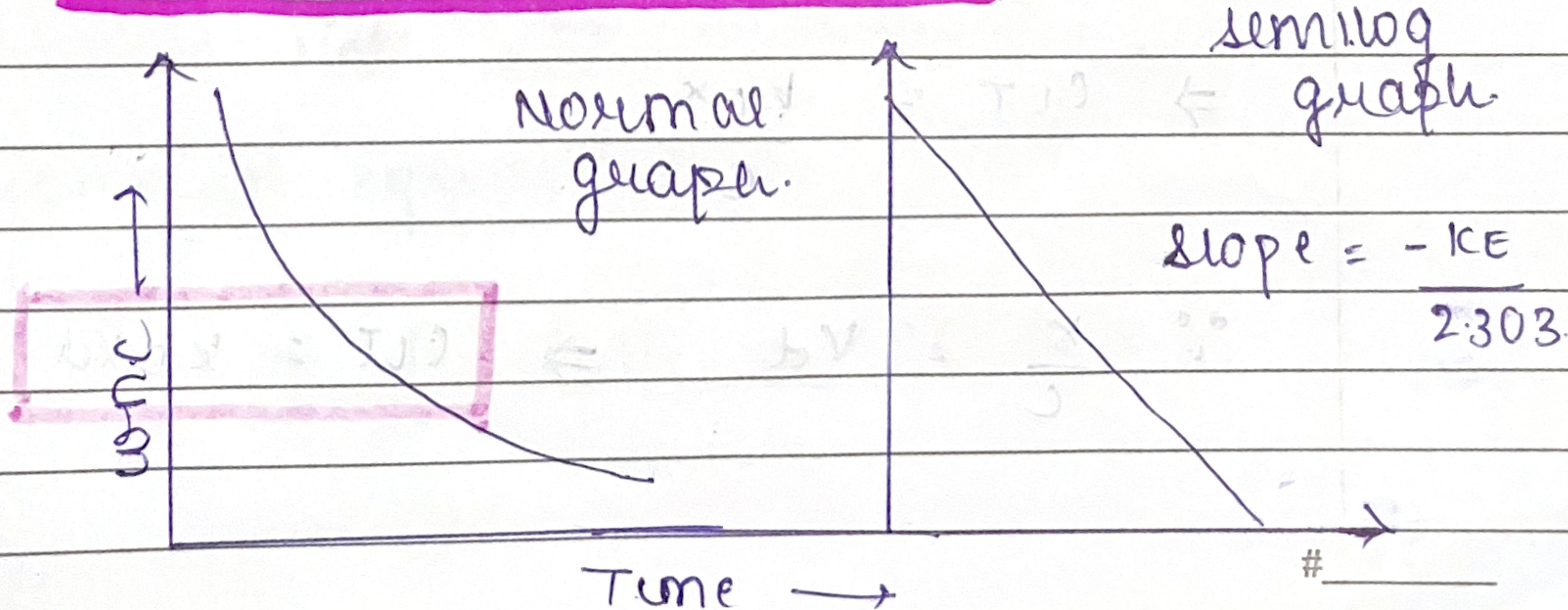
$$\log x = \log x_0 - \frac{k_{el} t}{2.303} \quad \text{--- (4)}$$

Hence,

$$x = C$$

$$x_0 = C_0$$

$$\log C = \log C_0 - \frac{k_{el} t}{2.303} \quad \text{--- (5)}$$





(2) Elimination half-life:

The time taken for the amount of drug in body as well as plasma concentration to decline to half of its initial value

$$t_{1/2} = \frac{0.693}{k_e}$$

(3) Clearance

Hypothetical volume of body fluids containing the drug which is completely removed in a given period of time.

$$Cl_r = \frac{\text{Rate of elimination}}{PDC}$$

$$= \frac{dx/dt}{C}$$

$$\therefore \frac{dx}{dt}$$

$$= k_e x$$

$$\Rightarrow Cl_r = \frac{k_e x}{C}$$

$$\therefore \frac{x}{C} = V_d$$

$$\Rightarrow Cl_r = k_e V_d$$

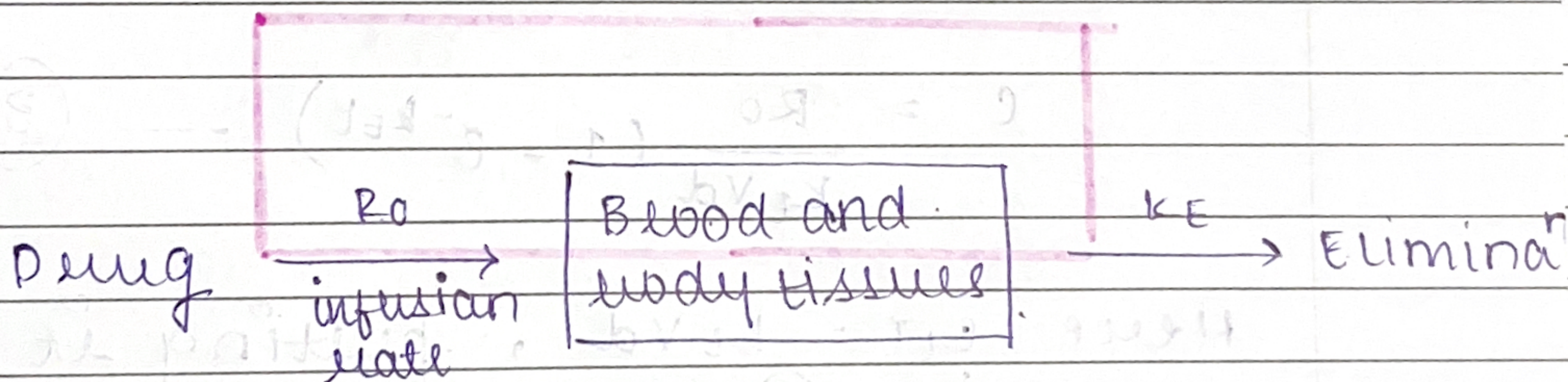


ONE COMPARTMENT OPEN MODEL (IV INFUSION):

- Sometimes, IV Bolus is inevitable where the drugs can precipitate toxicity.
- IV infusion is suitable when you require steady-state concentration. In such a situation, the drug is given at a constant rate (zero-order) by IV infusion.
- The half life ( $t_{1/2}$ ) of infusion longer than that of IV Bolus.

Advantages:

- (1) Ease of control of rate of infusion
- (2) Prevents fluctuating plasma levels
- (3) Other drugs, electrolytes and nutrients can be conveniently administered.



General equation.

$$\frac{dx}{dt} = \text{Rate in} - \text{Rate out}$$



$$\therefore \frac{dx}{dt} = R_0 - k_E x \quad \text{--- (1)}$$

Integrate the above equation --- (1)

$$x = \frac{R_0}{k_E} (1 - e^{-k_E t}) \quad \text{--- (2)}$$

By volume of distribution

$$x = v d c.$$

Putting values of  $x$  in (2), we get:

$$v d c = \frac{R_0}{k_E} (1 - e^{-k_E t})$$

$$c = \frac{R_0}{k_E v d} (1 - e^{-k_E t}) \quad \text{--- (3)}$$

Here  $c_{LT} = k_E v d$ , putting it in equation (3) we get:

$$c = \frac{R_0}{c_{LT}} (1 - e^{-k_E t}) \quad \text{--- (4)}$$



At steady-state, the rate of change of amount of drug in the body is zero  $\left( \frac{dx}{dt} = 0 \right)$

$$\therefore \frac{dx}{dt} = R_0 - k_e x$$

$$0 = R_0 - k_e x$$

But

$x = x_{ss}$  (steady state)

$$\therefore \boxed{0 = R_0 - k_e x_{ss}} \quad \text{--- (5)}$$

By rearranging the above equation, we get:

$$k_e x_{ss} = R_0$$

$$x_{ss} = R_0 / k_e$$

We know,  $x_{ss} = C_{ss}$

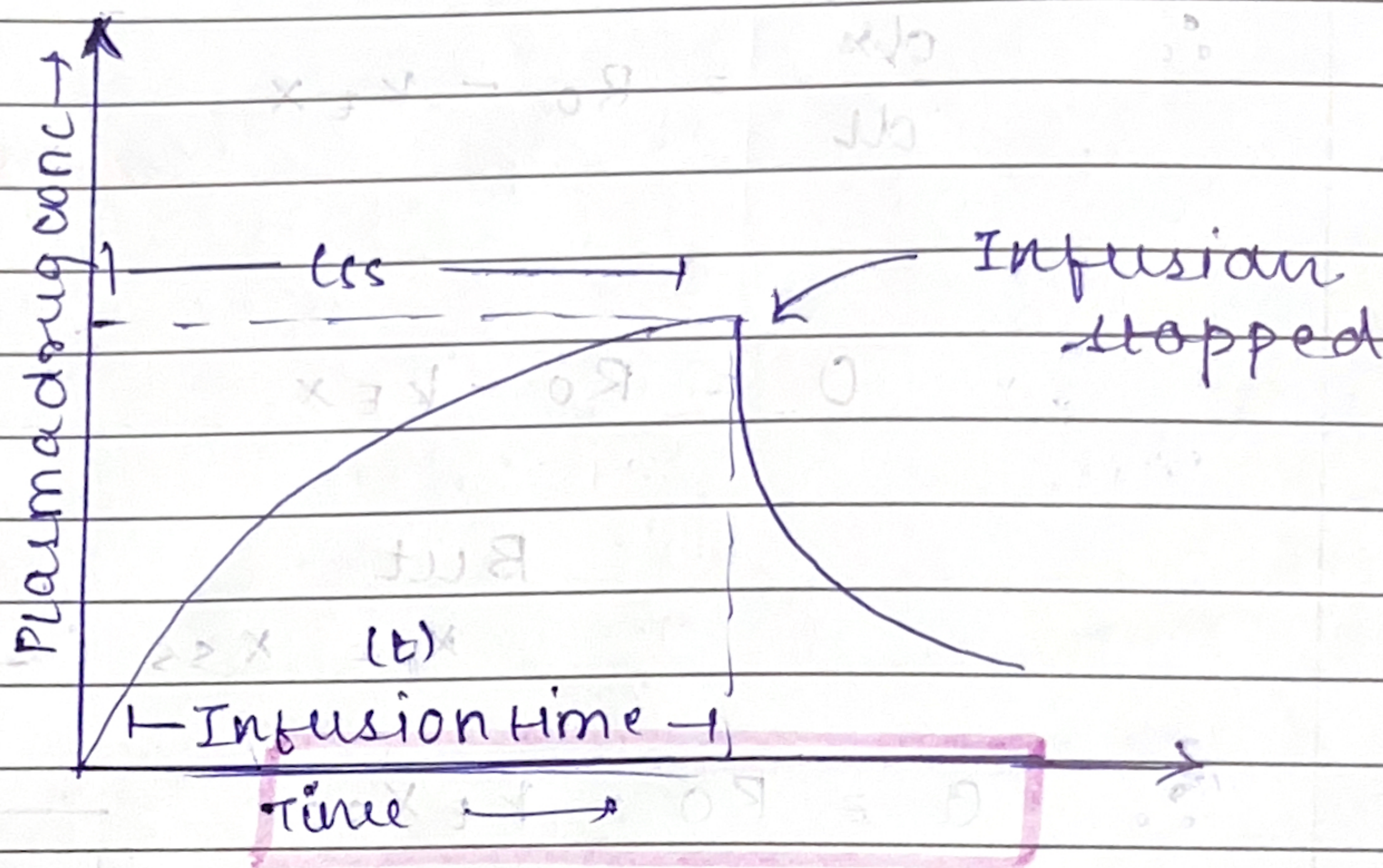
$$x_{ss} = V_d C_{ss}$$

$$\therefore C_{ss} = \frac{R_0}{k_e V_d} \Rightarrow k_e V_d = CL$$

$$\therefore \boxed{C_{ss} = R_0 / CL} \quad \text{--- (6)}$$



$$\Rightarrow C_{ss} = \frac{\text{Rate of infuse.}}{\text{Total clearance.}}$$



$$\text{slope} = \frac{-k_E}{2.303}$$

Pharmacokinetic parameters:

(1) Half life

$$t_{1/2} = 0.693 / k_E$$

$$(2) \text{slope} = \frac{-k_E}{2.303}$$

$$(3) AUC = \frac{R_0 T}{k_E V_d} = \frac{R_0 T}{C_{ss} \cdot T}$$

$$C_{ss} = R_0 / CL_T$$



# ONE COMPARTMENT OPEN MODEL EXTRAVASCULAR

## ADMINISTRATION :

- When a drug is given by an extra vascular route (oral, IM, Rectal etc) the absorption of the drug is prerequisite to its therapeutic activity.

OR

Rate of Absorption  $\propto$  Therapeutic activity of drug.

- It can be described mathematically

zero-order process

First-order process

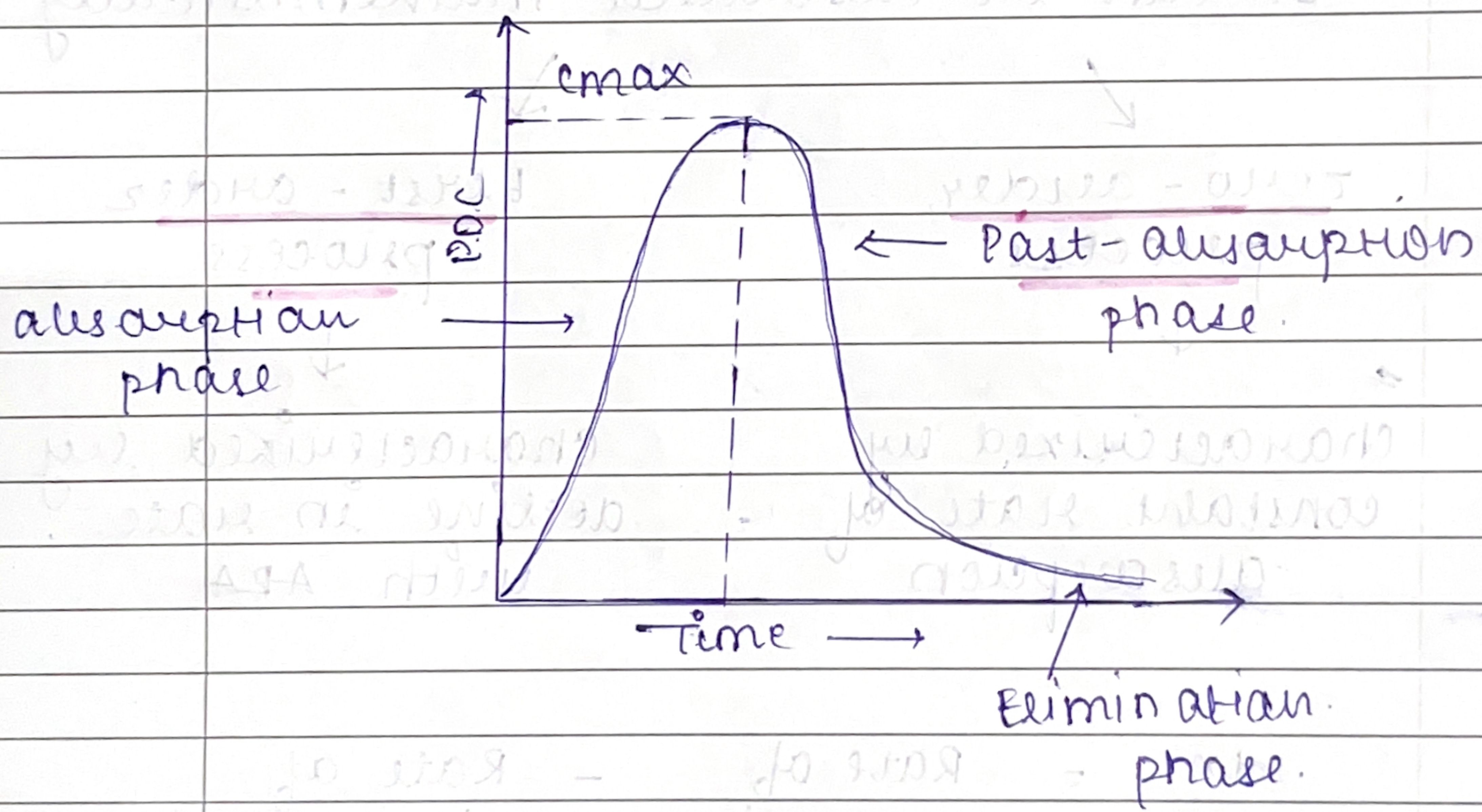
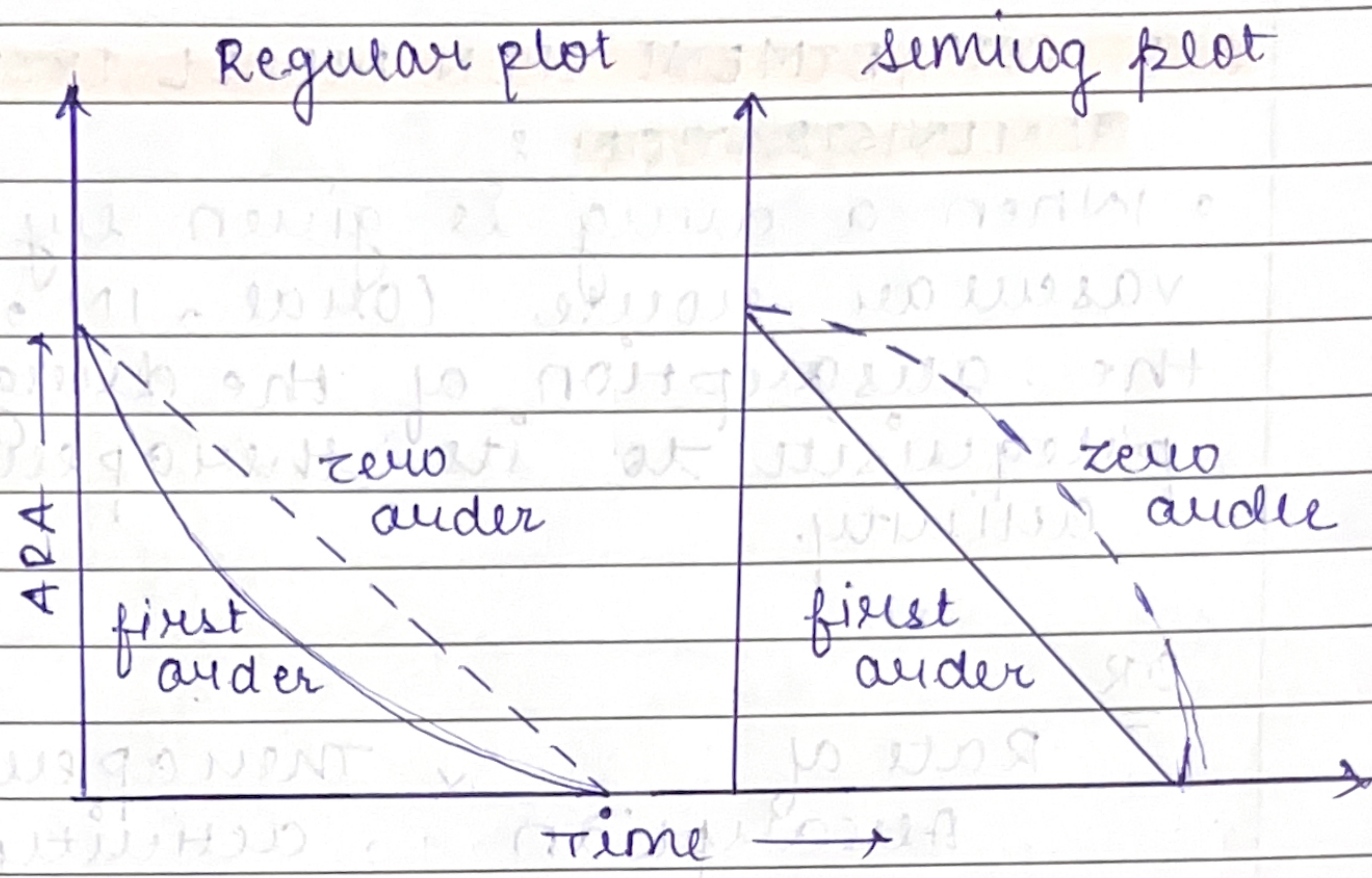
characterized by constant rate of absorption

characterized by decline in rate with ARA

$$\frac{dx}{dt} = \text{Rate of absorption} - \text{Rate of elimination}$$

$$\frac{dx}{dt} = \frac{dx_{ev}}{dt} - \frac{dx_E}{dt}$$





(1) Absorption phase.

$$\frac{dx_{ev.}}{dt} > \frac{dx_E}{dt}$$



(2) Post-absorption phase.

$$\frac{dx_{ev}}{dt} = \frac{dx_E}{dt}$$

(3) Elimination phase.

$$\frac{dx_{ev}}{dt} < \frac{dx_E}{dt}$$

⇒ Zero-order absorption:

Drug at  
ev site

$R_0$

↓

zero order.

Blood and  
other tissues

$k_E$ , Elimination

⇒ First-order absorption:

Drug at  
ev site

$k_a$

↓

first  
order

Blood and  
other tissues

$k_E$ , Elimination

From eq — (1)

$$\frac{dx}{dt} = k_a X_A - k_E X$$

(2)



Integrate equation (2) then we get:

$$x = \frac{k_a F X_0}{(k_a - k_e)} [e^{-k_e t} - e^{-k_a t}]$$

Transforming into terms of conc., we get:

$$C = \frac{k_a F X_0}{V_d (k_a - k_e)} [e^{-k_e t} - e^{-k_a t}]$$

(3)



**ABSORPTION RATE CONSTANT (Residual) :**

- It is used to resolve a multi-exponential curve into individual components.

For a drug that follows one-compartment kinetics and given

EV, the conc. of drug in plasma is expressed by a biexponential eqn.

$$C = \frac{k_a F X_0}{V_d (k_a - k_e)} [e^{-k_e t} - e^{-k_a t}] \quad \text{--- (1)}$$

If  $\frac{k_a F X_0}{V_d (k_a - k_e)} = A$ , a hybrid constant, then:

$$C = A e^{-k_e t} - A e^{-k_a t} \quad \text{--- (2)}$$

during elimination when absorption is almost over and the value of  $e^{-k_a t}$  approaches to zero, the eqn is reduced to:

$$\boxed{\bar{C} = A e^{-k_e t}} \quad \text{--- (3)}$$



When expressing eqn (3) in log form:

$$\log \bar{C} = \log A - \frac{k_E}{2.303}$$

where,

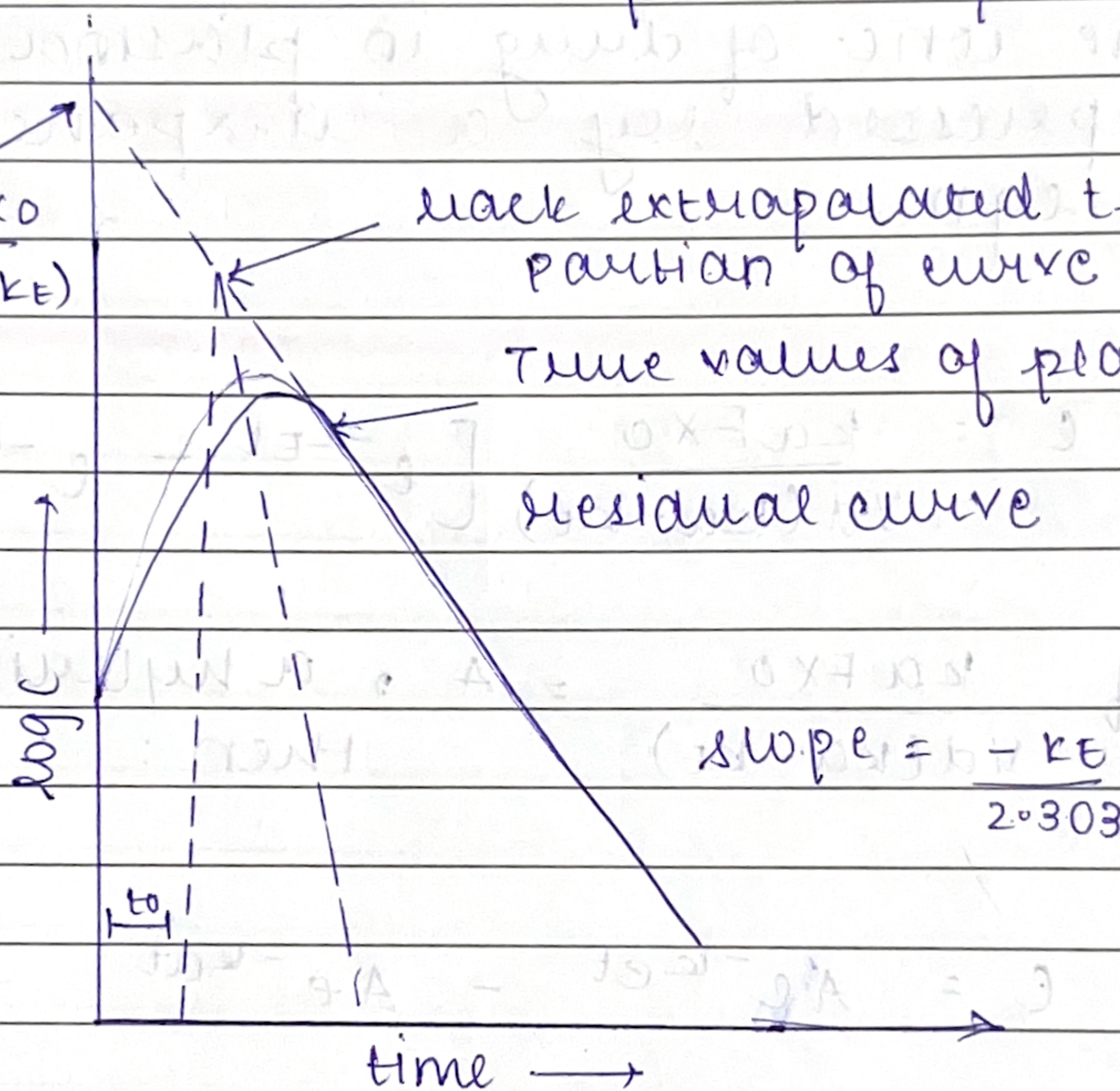
$\bar{C}$  = back extrapolated plasma

$$\log A = \log \frac{k_a F X_0}{V_d (k_a - k_E)}$$

back extrapolated terminal portion of curve ( $\log \bar{C}$ )

Time values of plasma conc.

residual curve



$$\log \bar{C} = \log A - \frac{k_E}{2.303}$$